

20th Section

1st Degree Price Discrimination

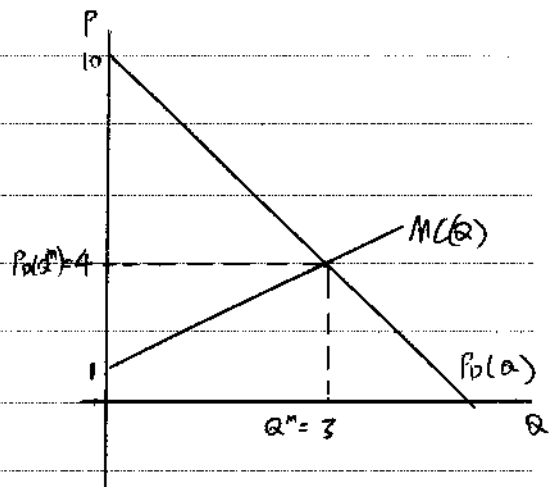
$$P_D(Q) = 10 - 2Q$$

$$MC(Q) = 1 + Q$$

Eq^m quantity : $P_D(Q^m) = MC(Q^m)$

$$10 - 2Q^m = 1 + Q^m$$

$$Q^m = 3$$



Price : Consumer who bought the Q^{th} unit pays $P_D(Q)$

Profit : $\pi(Q^m) = TS$ in competitive market

$$= \frac{1}{2} [P_D(0) - MC(0)] Q^m$$
$$= \frac{1}{2} (10 - 1) 3$$
$$= 13.5$$

CS : 0

Efficient outcome

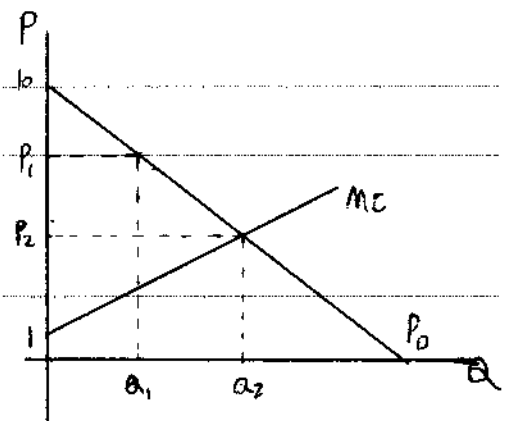
2nd Degree PD

Monopolist sets P_1, P_2, P_3, \dots

Buy less than Q_1 pays P_1 each,

Buy less than Q_2 pays P_2 each, etc.

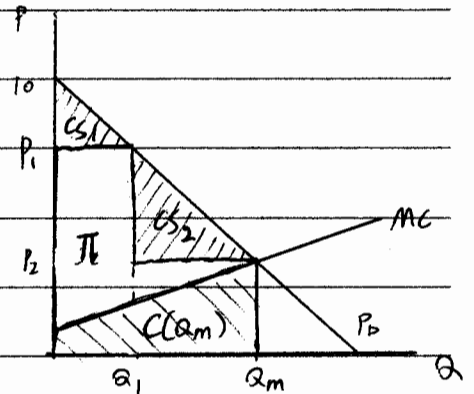
Suppose monopolist sets $P_1 = 6, P_2 = 4$



Eq^m quantity : $P_D(Q^m) = P_2$
 $Q^m = 3$

Profit : $\Pi = P_1 \cdot Q_1 + P_2 \cdot (Q_m - Q_1) - C(Q_m)$ area under MC
 $= 6 \cdot Q_D(6) + P_2 \cdot (3 - Q_D(6)) - (1+4) \cdot 3/2$
 $= 6 \cdot 2 + 4 \cdot (3 - 2) - 7.5$
 $= 8.5$

CS : $CS_1 + CS_2$
 $= \frac{1}{2}(P_D(0) - P_1) Q_1 + \frac{1}{2}(P_1 - P_2) Q_2$
 $= \frac{1}{2}(10 - 6) \cdot 2 + \frac{1}{2}(6 - 2) \cdot 1$
 $= 4 + 2$
 $= 6$



Efficiency : Depends on the last price (here is P_2) = MC
 or not. Efficient if yes ; not efficient otherwise.

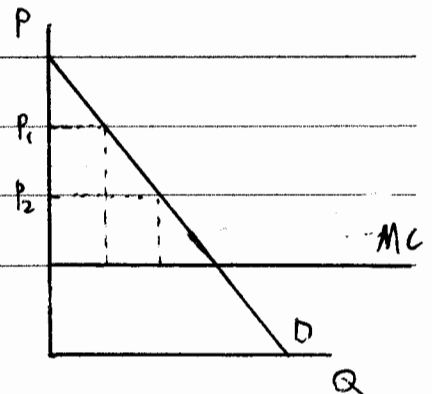
Rule - of - Thumb Pricing Rule for 2nd Degree PD

- Equally space the prices along the vertical intercept of demand and the free-market eq^m price P^c (given by $P_D = MC$).

i.e. $P_D(0) - P_1 = P_1 - P_2 = P_2 - P_3 = \dots = P_{n-1} - P_n = P_n - P^c = \frac{P_D(0) - P^c}{\# \text{ of } P + 1}$

$P^c = MC(Q \text{ free market}) = P_D(Q \text{ free market})$

Not efficient but better than single pricing.
 As # of prices $\rightarrow \infty$ its efficient



I think this holds for constant marginal cost only.

3rd Degree Price Discrimination

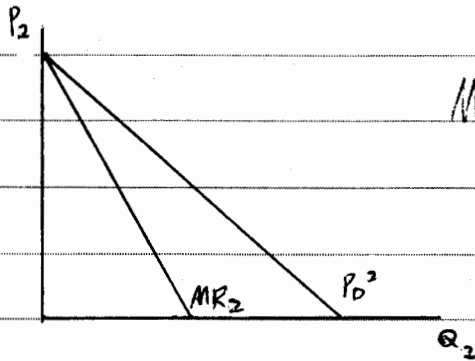
Monopolist can separate consumers into different groups.

Each group has its own demand curve and can be charged a different price (single price)

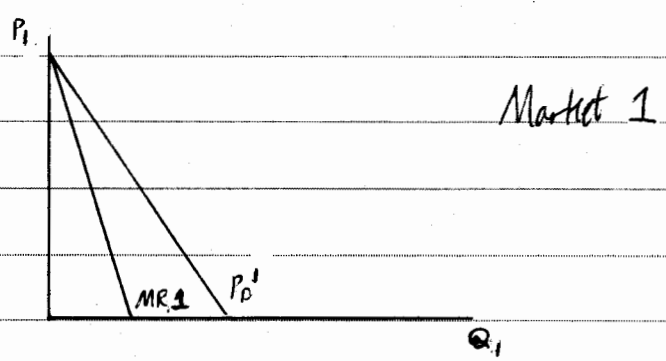
Cost depends only on total output.

Optimal Condition : $MR_1 = MR_2 = MC$

e.g. $P_D^2 = 10 - Q_2$



$$P_D^1 = 10 - 2Q_1$$



$$\begin{aligned} \text{Total cost : } C(Q_1 + Q_2) &= (Q_1 + Q_2) + \frac{(Q_1 + Q_2)^2}{2} + 5 \\ MC(Q_1 + Q_2) &= 1 + (Q_1 + Q_2) \end{aligned}$$

↑ fixed cost

$$MR_1 = 10 - 4Q_1, \quad MR_2 = 10 - 2Q_2$$

$$MR_1 = MR_2 = MC$$

$$10 - 4Q_1^m = 10 - 2Q_2^m = 1 + (Q_1^m + Q_2^m)$$

1. $10 - 4Q_1^m = 10 - 2Q_2^m$

$$2Q_1^m = Q_2^m$$

2. $10 - 4Q_1^m = 1 + (Q_1^m + Q_2^m)$

$$10 - 4Q_1^m = 1 + (Q_1^m + 2Q_1^m)$$

$$Q_1^m = \frac{9}{7}$$

3. $Q_2^m = \frac{18}{7}$

$$\text{Profit} : \pi = R_1 + R_2 - C$$

$$= P_D^1(Q_1^m) \cdot Q_1^m + P_D^2(Q_2^m) \cdot Q_2^m - C(Q_1^m + Q_2^m)$$

$$= \left[10 - 2\left(\frac{9}{7}\right)\right] \cdot \frac{9}{7} + \left[10 - \left(\frac{18}{7}\right)\right] \cdot \frac{18}{7} - \left[\left(\frac{9}{7} + \frac{18}{7}\right) + \frac{\left(\frac{9}{7} + \frac{18}{7}\right)^2}{2} + 5\right]$$

$$= 12.36$$

$$CS : CS_1 = \frac{1}{2} [P_D^1(0) - P_D^1(Q_1^m)] \cdot Q_1^m \quad (\text{Consumer Surplus in Market 1})$$

$$= \frac{1}{2} \left[10 - \frac{52}{7}\right] \cdot \frac{9}{7}$$

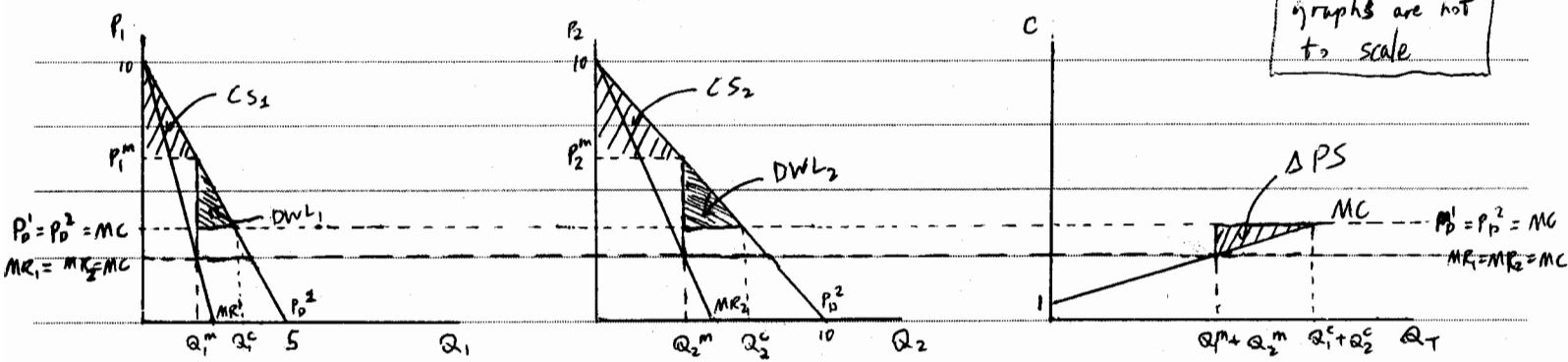
$$= 1.65$$

$$CS_2 = \frac{1}{2} [P_D^2(0) - P_D^2(Q_2^m)] \cdot Q_2^m \quad (\text{Consumer Surplus in Market 2})$$

$$= \frac{1}{2} \left[10 - \frac{52}{7}\right] \cdot \frac{18}{7}$$

$$= 3.31$$

$$\text{Total CS} = CS_1 + CS_2 = 4.96$$



$$\begin{aligned} \text{Deadweight loss} &= DWL_1 + DWL_2 + \Delta PS = \frac{1}{2} [P_1^m - MC(Q_1^c + Q_2^c)] \cdot (Q_1^c - Q_1^m) \\ &\quad + \frac{1}{2} [P_2^m - MC(Q_1^c + Q_2^c)] \cdot (Q_2^c - Q_2^m) \\ &\quad + \frac{1}{2} [MC(Q_1^c + Q_2^c) - MC(Q_1^m + Q_2^m)] \cdot [(Q_1^c + Q_2^c) - (Q_1^m + Q_2^m)] \\ &= 0.264 + 0.529 + 1.190 = 1.984 \end{aligned}$$

Inefficient, but still better than single-pricing.

$$\text{Note that since } \frac{P_i - MC}{P_i} = -\frac{1}{\epsilon_{d_i}}, \quad P_1/P_2 = \frac{1 + 1/\epsilon_{d_1}}{1 + 1/\epsilon_{d_2}}$$

In our case $\frac{P_1}{P_2} = 1$, but this is a special case. In general, lower demand elasticity $\epsilon_{d_i} \Rightarrow$ higher price P_i^m